The Spin Probe Dynamics and the Free Volume in a Series of Amorphous Polymer Glass-Formers

H. Švajdlenková, M. Iskrová, O. Šauša, G. Dlubek, J. Krištiak, J. Bartoš *1

Summary: We report the results of a combined study of the local structure and the reorientation dynamics in a series of five amorphous polymers of different fragility: cis-trans-1,4-poly(butadiene) (c-t-1,4-PBD), cis-1,4-poly(isoprene) (cis-1,4-PIP), poly(isobutylene) (PIB), poly(vinyl methylether)(PVME) and poly (propylene glycol) (PPG) by using two different probe methods. The reorientation dynamics of the molecular spin probe 2,2,6,6-tetramethyl-1-piperidinyloxy (TEMPO) from electron spin resonance (ESR) is related to the annihilation behaviour of the atomic ortho-positronium (o-Ps) one as obtained by positron annihilation lifetime spectroscopy (PALS). It was found that a slow to fast transition in the spin probe rotation mobility at the operationally defined spectral temperature parameter, T_{50G} , is connected with the mean o-Ps lifetime, τ_3 $(T_{SOG}) = (2.04 \pm 0.26)$ ns. Consequently, using the free-volume concept of the o-Ps annihilation in terms of a quantum-mechanical model of o-Ps lifetime this transition can be connected with the occurrence of the mean free volume hole, V_h $(T_{SOG}) = (102 \pm 17) \text{ Å}^3$, nearly independent of the chemical composition and the basic structural relaxation parameters of the amorphous polymers investigated. Finally, the free volume hole distribution aspect of the slow to fast transition indicates the presence of a sufficient free volume fluctuation at T_{50G} for both typical fragile PVME and strong PIB polymer and emphasizes the essential role of free volume in the spin probe dynamics.

Keywords: amorphous polymers; ESR; free volume; PALS; spin probe reorientation

Introduction

The structure and dynamics of glassformers can be investigated via the socalled "reporter" molecular probe techniques such as stable free radicals using electron spin resonance (ESR).

The spectral evolution of the triplet signal from the spin probe of nitroxide type in a given condensed matrix reflects its rotational dynamics which is influenced by the internal factors such as the matrix properties, i.e., chemical composition, physical microstrucThe physical structure and dynamics of disordered systems is often discussed using the free volume concept. ^[4,5] In the past this idea was utilized to interpret the spin probe dynamics by formulating the various versions of free volume models of spin-probe rotation in polymers without their direct experimental verification. ^[6–8] Recent progress in positron annihilation lifetime spectroscopy (PALS) methodology allows to obtain the free volume information from the annihilation behavior of the atomic-sized probe, the ortho-positronium (o-Ps) in condensed materials. ^[9,10]

In this contribution we present a combined ESR and PALS study on a series of

ture and its static and dynamic fluctuations, the spin probe parameters such as its size and shape as well as by the external ones such as temperature etc. ^[1–3]

Polymer Institute, Slovak Academy of Sciences, Dúbravská cesta 9, 845 41 Bratislava, Slovakia E-mail: Jozef.Bartos@savba.sk

² Institute of Physics, Slovak Academy of Sciences, Dúbravská cesta 9, 842 28 Bratislava, Slovakia

³ ITA Institute for Innovative Technologies, Köthen/ Halle, Wiesenring 4, 06120 Lieskau, Germany

five amorphous polymers aimed to clarify the role of the measured free volume factor in the spin probe rotation dynamics.

Experimental Part

Materials

Five amorphous polymeric glass formers were selected for experiments. They included the structurally simple homopolymers of diene type without side group cistrans-1,4-poly(butadiene) (c-t-1,4-PBD) and with side group cis-1,4-poly(isoprene) (c-1,4-PIP), of vinyl type poly (vinyl methyl ether) (PVME) and of vinylidene type poly(isobutylene) (PIB) as well as one typical heteropolymer poly (propylene glycol) (PPG) (Figure 1). The values of molecular weight and basic thermodynamic (glass transition temperature) and dynamic, i.e., structural relaxation and related fragility [11] parameters are listed in Table 1.

As the spin probe the stable nitroxyltype radical 2,2,6,6-tetramethyl-1- piperidinyloxy (TEMPO) from Aldrich, Inc. was used. The molecular structure of quasispherical molecule of TEMPO is also given in Figure 1. Basic molecular parameters of spin probe TEMPO, i.e., van der Waals volume $V_{TEMPO}^{W} = 170.1 \text{ Å}^3$ corresponding to the equivalent radius of $R_{eq}^{W} = 3.45 \text{ Å}$ was obtained using the simulation software Cerius², Accelrys, Inc., San Diego.

Sample Preparation

The soft solid matrices were prepared by diffusion of the vapor of the *TEMPO* at elevated temperature. The liquid matrices were prepared by dissolution of the *TEMPO* in a given matrix at concentration of about 10^{-3} spin $\,\mathrm{mol}^{-1}$.

Electron Spin Resonance

ESR measurements were carried out on the X-band Bruker-ER 200 SRL with a Bruker BVT100 temperature variation controller unit. The ESR spectra were recorded over a wide temperature range from $100\,\mathrm{K}$ up to $370\,\mathrm{K}$. The ESR spectra of all the amorphous *polymer/TEMPO* systems have been evaluated in terms of the spectral parameter of mobility, $2A_{zz'}$, (see Figure 2) as a function of the temperature.

Positron Annihilation Spectroscopy

PALS investigations on *c-t-1,4-PBD*, *PPG* and *PVME* were carried out by the Bratislava's group, Slovakia and on *c-1,4-PIP* and *PIB* by the Halle's team, Germany. The

Figure 1.

Chemical structures of polymer matrices: cis-trans-1,4-poly(butadiene) (c-t-1,4-PBD), cis-1,4-poly(isoprene) (c-1,4-PIP), poly(vinyl methyl ether) (PVME), poly(isobutylene)(PIB) and poly(propylene glycol) (PPG) as well as of spin probe TEMPO.

Table 1. The polymer and polymer/TEMPO parameters: molecular weight, M_n , glass-liquid transition temperature from DSC, T_g , fragility, m_g , $^{[1]}$ characteristic ESR temperature, T_{50G} and mean o-Ps lifetime, $\tau_3(T_{50G})$. $^{[12-16]}$

Polymer	M _n Da	T _g K	m _g -	T _{50G} K	T _{50G} /T _g -	τ ₃ (T _{50G}) ns	Ref.
c-t-1,4-PBD	2.2×10^{3}	174	84	224	1.29	2.06	12
PPG	4×10^3	198	83	242	1.21	2.17	13
c-1,4-PIP	8×10^{5}	200	65	255	1.28	2.26	14
PIB	1×10^6	205	46	263	1.29	1.78	15
PVME	3.7×10^{4}	250	75	276	1.11	1.98	16

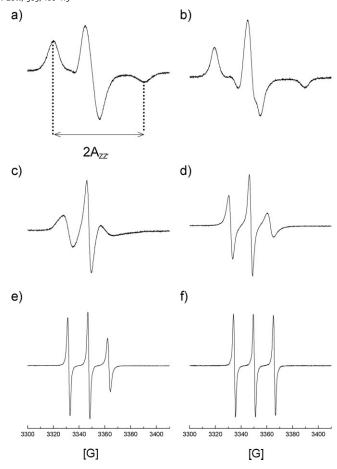


Figure 2.

Spectral evolution as a function of the temperature for the PPG/TEMPO system at a) 100 K, b) 200 K, c) 250 K, d) 275 K, e) 300 K and finally, f) 350 K.

details of both experimental set up and evaluation procedures of the PALS spectra can be found in Refs. [17,18].

Results and Discussion

ESR Data

The typical ESR spectral evolution of the spin probe *TEMPO* with temperature is similar for all the investigated *polymer/TEMPO* systems as it is illustrated by the *PPG/TEMPO* case in Figure 2. The triplet spectrum changes from a broad signal at lower temperatures to a narrow one in higher temperature region. This corresponds to a dynamic change of the *TEMPO*

from the slow motional regime with the higher values of the spectral parameter of mobility $2A_{zz}$, ~ 70 –65 G to the fast motional regime with the lower ones $2A_{zz}$, ~ 35 –30 G.

The spectral parameter of *TEMPO* mobility, $2A_{ZZ'}$, as a function of temperature in our series of five amorphous polymers is presented in Figure 3. Typical sigmoidal dependence with a characteristic transition from the slow to fast motional regime is operationally quantified by the spectral temperature parameter T_{50G} [19] (Table 1). For all the investigated *polymer/TEMPO* systems the T_{50G} values lie about 10–30% above the basic thermodynamic parameter of polymer glass-formers, i.e. the

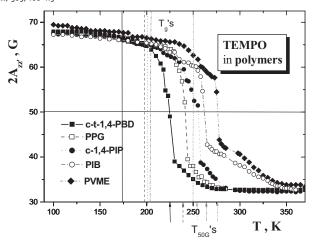


Figure 3. Spectral parameter of mobility, $2A_{ZZ'}$, as a function of the temperature of *TEMPO* in a series of amorphous polymers. The glass-liquid temperatures, T_{g} , are depicted by the vertical lines and the characteristic ESR temperature, T_{SOG} , are marked by the arrows; both the quantities are summarized in Table 1.

corresponding glass - liquid transition temperatures, T_{ρ} .

By inspection of the further basic dynamic parameter of glass-forming systems, i.e. fragility, mg, [11] characterizing the temperature dependence of the structural relaxation of glass-formers, we find that the strongest polymer PIB with $m_g = 46$ exhibits the relative transition temperature T_{50G}/ $T_{\sigma} \sim 1.29$ being nearly the same as that for the most fragile polymer c-t- 1,4-PBD among the used matrices with the essentially higher values of fragility: $m_g = 84$. This implies that no direct relationship between the slow to fast transition of the spin probe TEMPO and the structural relaxation process is observed. Then, another physical factor has to control the slow to fast transition of the spin probe TEMPO.

PALS Data

Positron annihilation lifetime spectroscopy (PALS) is a unique method to *direct* observation of free space in condensed matrices. [9,10,18] The principle of PALS consists in detecting the annihilation of the atomic-sized ortho-positronium (o-Ps) probe, i.e., a bound system of one positron, e+, and one electron, e-, with the mutually parallel spins which is trapped in the regions of low electron density, the so-

called free volume. The positron lifetime spectrum of condensed materials is usually a sum of three exponentially decaying channels with its characteristic lifetime values from 1) para - positronium (p-Ps, $\tau_1 \sim 125 \, \mathrm{ps}$), 2) "free"positron (e+, $\tau_2 \sim 300-500 \, \mathrm{ps}$) and finally, 3) ortho - positronium (o-Ps, $\tau_3 \sim 1-5 \, \mathrm{ns}$). In practice, the PALS spectra are evaluated by the PATFIT program^[20] providing the mean o-Ps lifetime values and also using the MELT or LT 9.0 routines^[21,22] to obtain the o-Ps lifetime distribution and the related free volume distribution functions.

In the framework of free volume interpretation of the o-Ps annihilation in condensed matter and the standard quantum-mechanical model of o-Ps annihilation in spherical free volume hole, the o-Ps lifetime, τ_3 , is related to the free volume hole size, R_h , as follows: [23]

$$\tau_3 = \tau_{3,0} \{ 1 - R_h / (R_h + \Delta R) + (1/2\pi) \sin[2\pi R_h / (R_h + \Delta R)] \}^{-1}$$
 (1)

where $\tau_{3,0}$ is the spin averaged lifetime of p-Ps and o-Ps equals to 0.5 ns and $\Delta R = R_0 - R_h = 1.66 \text{ Å}$ is the thickness of electron layer about free volume hole obtained as a parameter from fitting the observed o-Ps lifetimes to known vacancy or free volume

hole sizes in molecular crystals and zeolites.^[23] In reality, the shape of free volume entities is not spherical, so that the standard model (Eq. 1) is used in the sense of the mean o-Ps lifetime and subsequently, to estimate the equivalent mean hole radius. Then, the corresponding mean hole volume is given $V_h = (4/3) \pi R_h^3$. Moreover, in any real disordered material a distribution of free volume holes is present giving the corresponding distribution of o-Ps lifetimes. Then, if one-to-one correspondence between the o-Ps lifetime and the freevolume hole radius is valid, the o-Ps lifetime distribution from MELT or LT programs can be transformed into the freevolume hole radius distribution, Eq. 2:

$$f(R_h) = -2\Delta R \left\{ \cos \left[2\pi \left(\frac{R_h}{R_0} \right) \right] - 1 \right\} \frac{\alpha(\lambda_3)}{R_0^2}$$

and finally, $f(R_h)$ can be converted into a free-volume distribution function, eq 3:

$$g(V_h) = \frac{f(R_h)}{4 \pi R_h^2}$$
 (3)

Next, a role of the local free volume in the rotational dynamics of the spin probe *TEMPO* in our series of amorphous polymers from ESR investigations will be evaluated from both the phenomenological and geometrical points of view.

Phenomenological Relationship between the ESR and PALS Databases

The mean o-Ps lifetimes, τ_3 , as a function of temperature, T, for the same five amorphous polymers used in ESR study are plotted together in Figure 4. In all the investigated polymer glass-formers a typical sigmoidal form of τ_3 vs. T dependence is observed. The detailed τ_3 vs. T plot is displayed for the case of poly(vinyl methylether) in Figure [16]. The existence of several regions of distinct thermal behavior of τ_3 can be found by a linear fitting procedure [12,15]. Basically, three significantly distinct regions with the two characteristic PALS temperatures can be revealed: the first most pronounced effect at lower T's is connected with the glass to supercooled liquid transition at T_g^{PALS} and the other one in higher T region marked by a plateau or quasi-plateau level tendency is connected with supercooled to normal liquid transition at $T_{b2}^L \sim (1.4$ -1.75)xT^{PALS} [12,13,15]. In addition, more or less slighter bend effect depending on the matrix fragility at $T_{b1}^G \sim (0.5\text{--}0.7)xT_{\sigma}^{PALS}$

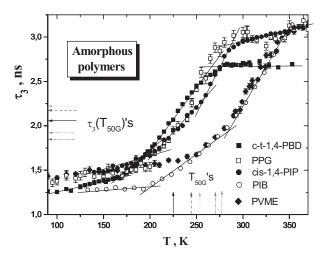


Figure 4. The mean o-Ps lifetime, τ_3 , as a function of the temperature for a series of pure amorphous polymers. The arrows depict the values of o-Ps lifetimes τ_3 (T_{50G}) corresponding to the spectral temperatures T_{50G} for TEMPO from Figure 3.

and $T_{b1}^L \sim (1.2$ - $1.4)xT_g^{PALS}$ which mark the presence of two various glass or supercooled liquid regions can be distinguished. $^{[12,15]}$ The τ_3 values and their changes with T over more or less extended T range reflect differences in the free volume microstructure depending on the chemical and physical, i.e. free volume, structure and the dynamics of various polymers. $^{[9,10,12,18]}$

In the context with our ESR results in Figure 3, the most remarkable empirical finding is that the o-Ps lifetime, $\tau_3(T_{50G})$, corresponding to the most pronounced effect in 2A_{ZZ} vs. T plot i.e. the slow to fast transition in the spin probe TEMPO dynamics, are in a relative narrow range (Table 1) characterized by the average value: $\tau_{3,ave}$ (T_{50G}) = (2.04 ± 0.25) ns. Thus, a change of the spin probe TEMPO between the two basic motional regimes is associated with the mean o-Ps lifetime being almost independent of the chemical composition and the fragility of the polymer matrices used. From Eq. 1 this corresponds to the mean free volume $V_{h,ave} = (102 \pm 17) \text{ Å}^3$. This finding can be interpreted in such a way that the spin probe TEMPO transition occurs at the presence of the average free volume reaching about 60% of van der Waals volume of *TEMPO*, $V^W = 170.1 \text{ Å}^3$.

In addition, in connection with our combined ESR and PALS approach we find some further mutual coincidences between various discontinuity effects in the ESR or PALS response as it is demonstrated for *PVME* (Figure 5). They include the following relations between the corresponding characteristic ESR and PALS temperatures: $T_{X1}^G \cong T_{b1}^G$ and T_{X2}^G $\approx T_g^{PALS}$ in the slow regime, $T_{50G} \approx T_{b1}^{L}$ and $T_{X2}^L \cong T_{b2}^L$ in the fast one. These coincidences suggest the similar origin of underlying dynamic processes which cause both the significant changes in the reorientation of molecular spin probe *TEMPO* as well as in the annihilation of the atomic o-Ps probe. Detailed discussion of these effects requires the further relevant dynamic information exceeding the extent of this paper and this aspect will be published elsewhere.

Geometrical Relationships between the Spin Probe *TEMPO* and Free Volume Hole Distribution

Another level of the ESR and PALS analysis consists in a direct comparison of the spin probe *TEMPO* size with the detailed free volume hole microstructure as obtained from the continuous analysis of

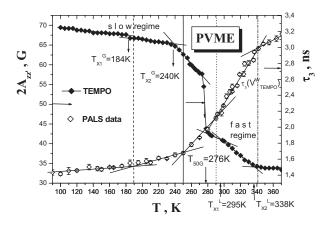


Figure 5. Comparison of the spectral parameter of TEMPO mobility, $2A_{ZZ,}$ with the mean o-Ps lifetime, $τ_3$, for the PVME sample as a function of the temperature. The characteristic ESR temperatures: $T_{X_1}^G = 184$ K, $T_{X_2}^G = 240$ K, $T_{50G} = 276$ K, $T_{X_1}^L = 295$ K and $T_{X_2}^L = 338$ K are related to the characteristic PALS ones depicted by vertical lines as follows: $T_{X_1}^G \cong T_{b_1}^G = 190$ K (dash), $T_{X_2}^G \approx T_g^{PALS} = 250$ K (solid), $T_{50G} \approx T_{b_1}^L = 290$ K (dot) and $T_{X_2}^L \cong T_{b_2}^L = 342$ K (dash-dot).

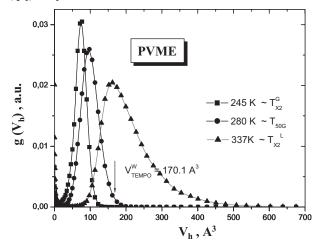


Figure 6. Relationships between the free volume distributions $g(V_h)$ at the selected temperatures 245 K, 280 K and 337 K close to the characteristic ESR ones from Figure 5 for PVME. The arrow depicts the van der Waals volume of the spin probe *TEMPO*, V_{TEMPO}^W .

the PALS spectra by using the MELT or LT programs. [15,16]

Figure 6 shows a relationship between the van der Waals volume of the TEMPO. V_{TEMPO}^{W} , and the free volume hole distributions g(V_h) in the relatively fragile PVME sample as obtained from Eq. 3 at several temperatures close to the characteristic ESR ones in Figure 4 using the program MELT. In general, when the temperature increases, g(Vh) moves to the larger values and at the same time broadens. The van der Waals volume of TEMPO, VWTEMPO, is depicted by the arrow also. At low temperature, $T = 245 \, \text{K}$, the $V_{\text{TEMPO}}^{\text{W}}$ lies outside of the corresponding hole volume distribution. This indicates that in the slow regime the spin probe TEMPO forms a certain type of structural perturbation of the PVME matrix and moves due to very small fluctuation in its surrounding. On increase the temperature, the free volume hole distributions g(Vh) approaches the vdW volume of the spin probe TEMPO and at T_{50G} the high-value tail of the g(V_h) reaches just the V^W_{TEMPO} value. Thus, the spin probe TEMPO at the T_{50G} has a sufficient local free space for the pronounced change in its rotation dynamics in the PVME matrix. This indicates that a transition of the spin probe *TEMPO* from the slow to rapid regime appears to be associated with the occurence of a local free volume fluctuation in the surrounding PVME matrix.

Finally, at higher temperatures, the crossover effect within the fast motional regime of the spin probe TEMPO at T_{X2}^L (Figure 5) appears to be associated with the maximum of $g(V_h)$ which corresponds to the maximal probability of the occurrence of free volume holes being nearly equal to the V_{TEMPO}^W . Recently, similar findings were reported also for a typical strong member from our series of the investigated polymer glass-formers samples - poly (isobutylene) (PIB). [24]

Thus, the observed relationships between the changes in spin probe *TEMPO* reorientation and the free volume fluctuation suggest on their close mutual connections independently of the chemical composition, the structural relaxation and the related strong or fragile dynamic character of the polymer glass-former.

Conclusion

The rotational dynamics of the spin probe *TEMPO* in a series of polymer glass-formers

of different chemical composition, glass transition temperature and fragility has been related to the annihilation behavior of the atomic o-Ps probe and the closely related free volume microstructure information as obtained from the PALS studies. Thus, a joint ESR and PALS approach enables to obtain better understanding of the relative role of various physical factors controlling the reorientation dynamics of small molecules in the various polymer matrices.

Acknowledgements: This work was supported by the VEGA Agency, Slovakia under Grants No. 2/0014/09 (J.B.) and 2/0099/10 (O.Š.).

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